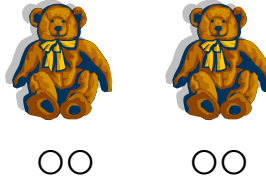




Multiplication

To begin with, children learn about equal groups

Equal groups in circles; equal groups with markers eg teddy bears; equal groups without markers



Children also learn to count rhythmically or to skip count

Example ○○ ○○
 1 2 3 4

When they do this, they add the same number all the time

Example 2 4 6 8
 +2 +2 +2

When children are in year 3, they are ready to learn how to multiply numbers

Children begin by investigating multiplication by 2, 4, 3, 10 and 5 (not times tables)

Then, multiplication by 8, 6, 9 and 7 (not times tables)

Students are asked to imagine a number that is 2 times bigger (double); 4 times bigger (double and double again); 3 times bigger; 6 times bigger etc

*Learning times tables isn't enough because
we want children to be able to multiply large numbers*





Distributive property of multiplication

Distributing multiplication over addition

*(children can partition numbers they **can't** multiply, into numbers they **can** multiply and then add the products)*

Example (single digit)

$$\begin{array}{r} 2 \times 7 = 14 \\ \swarrow \searrow \\ 2 + 5 \end{array}$$

$$2 \times 2 = 4 \text{ (is the product)}$$

$$2 \times 5 = 10 \text{ (is the product)}$$

$$\text{So, } 4 + 10 = 14$$

This can work with teen numbers and 2 digit numbers

Example (teen number)

$$\begin{array}{r} 2 \times 14 = 28 \\ \swarrow \searrow \\ 10 + 4 \end{array}$$

$$2 \times 10 = 20$$

$$2 \times 4 = 8$$

$$\text{So, } 20 + 8 = 28$$

Example (2 digit number)

$$\begin{array}{r} 2 \times 45 = \\ \swarrow \searrow \\ 40 + 5 \end{array}$$

$$2 \times 40 = 80$$

$$2 \times 5 = 10$$

$$\text{So, } 80 + 10 = 90$$



Children can partition either number

Example

$$\begin{array}{c} 4 \times 13 = 52 \\ \swarrow \quad \searrow \\ 2 \quad 2 \end{array}$$

$$2 \times 13 = 26$$

$$2 \times 13 = 26$$

So, $26 + 26 = 52$

OR

$$\begin{array}{c} 4 \times 13 = 52 \\ \swarrow \quad \searrow \\ 10 \quad 3 \end{array}$$

$$4 \times 10 = 40$$

$$4 \times 3 = 12$$

So, $40 + 12 = 52$





Multiplicative place value

When a number is multiplied by 10, it moves one column to the left

thousands	hundreds	tens	ones
			1
		1	0
1	0	0	0

Using multiplicative place value

Example $4 \times 56 = 224$

$$\begin{array}{l} \swarrow \quad \searrow \\ 50 + 6 \end{array}$$

$$4 \times 50 =$$

same as $4 \times 5 \times 10 =$

same as $20 \times 10 =$

When a number is multiplied by 10, it moves one column to the left

hundreds	tens	ones
	2	0
2	0	0

So, 20×10 becomes 200

Back to multiplying $4 \times 56 = 224$

$$4 \times 50 = 200$$

$$4 \times 6 = 24$$

So, $200 + 24 = 224$





Multiplying by 5

Example

$$5 \times 8 = 40$$

Start with 10×8 (which we know) = 80

Then halve 80

$$\frac{1}{2} \text{ of } 80 = 40$$

So, $5 \times 8 = 40$

Multiplying by 9

Example

$$9 \times 7 = 63$$

Start with $10 \times 7 =$ (which we know) = 70

10×7 is 1×7 more than 9×7

So, $70 - 7 = 63$

